Orange Public Schools

Office of Curriculum & Instruction 2019-2020 Mathematics Curriculum Guide



Second Grade Mathematics

Unit 1:

Eureka - Module 1: Sums and Differences to 20 September 9, 2019 – September 27, 2019

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Yearlong Pacing Guide: Second Grade

Eureka Math	Eureka Module Standards
Unit 1- Module 1: Sum/ Difference to 20 Sept 9- Sept 27	20A1, 20A2, 2NBT5
Unit 2-Module 2: Add/ Subtract Length Sept 30- Oct 18	2MD1, 2MD2, 2MD3, 2MD4, 2MD5,2MD6
Unit 3- Module 3: Place Value, Count to 1000 Oct 21 – Nov 26	2NBT1, 2NBT2, 2NBT3, 2NBT4
Unit 4- Module 4: Add/ Subtract within 200 (Word Problems up to 100) Dec 2- Jan 31	20A1, 2NBT5, 2NBT6, 2NBT7. 2NBT8, 2NBT9
Unit 5- Module 5: Add/ Subtract within 1000 (Word Problems up to 100) Feb 3- March 13	<mark>2NBT7, 2NBT8, 2NBT9</mark>
Unit 6- Module 7: Length, Money, Data March 16- May 8	2NBT5, 2MD1, 2MD2, 2MD3, 2MD4, 2MD5, 2MD6, <mark>2MD8, 2MD9, 2MD10</mark>
Unit 7- Module 8: Time, Shapes, Fractions May 11- June 5	<mark>2MD7, </mark> 2G1, 2G3
Unit 8- Module 6: Foundations Multiplication Division June 8- EOSY	<mark>20A3, 20A4</mark> , <mark>2G2</mark>

References

"Eureka Math" Gt Minds. 2018 < https://greatminds.org/account/products

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Module 1		
Essential Questions	Enduring Understandings	
 How does the position of a digit in a number affect its value? In what different ways can numbers be grouped? How can memorizing the basic addition and subtraction facts help me? How does understanding place value help you solve double digit addition and subtraction problems? What are efficient methods for finding sums and differences? 	 Knowledge of addition and subtraction facts makes the computation of larger numbers easier to solve. Numbers can be aligned in accordance with place value to correctly add denominations of ten. Flexible methods of computation involve grouping numbers in strategic ways. Mental math strategies can be used to solve prob- lems involving numbers. 	

Performance Overview

- Topic A's two lessons are devoted solely to the important practice of fluency, the first lesson working within 20 and the second extending the same fluencies to numbers within 100.
- Topic A reactivates students' Kindergarten and Grade 1 learning as they energetically practice the following prerequisite skills for Level 3 decomposition and composition methods
- Topic B takes Grade 1's work to a new level of fluency as students make easier problems to add and subtract within 100 by using the number system's base ten structure. The topic begins with students using place value understanding to solve problems by adding and subtracting like units (e.g., "I know 8 5 = 3, so 87 50 = 37 because 8 tens 5 tens = 3 tens. I know 78 5, too, because 8 ones 5 ones = 3 ones. I used the same easier problem, 8 5 = 3, just with ones instead of tens!"). Students then practice making ten within 20 before generalizing that strategy to numbers within 100 (e.g., "I know 9 + 6 = 15, so 79 + 6 = 85, and 89 + 6 = 95").

	Modul	e 1: Sums and Differences to 20		
		<u>Pacing:</u>		
September 9, 2019- September 27, 2019				
Suggested Instructional Days: 15				
Торіс	Lesson	Student Lesson Objective/ Supportive Videos		
Topic A:	Lesson 1	Practice making ten and adding to ten. https://www.youtube.com/watch?v		
Foundations for Fluency with Sums and Differences within 100	Lesson 2	Practice making the next ten and adding to a multiple of ten. https://www.youtube.com/watch?v		
Topic B:	Lesson 3	Make a ten to add within 20. https://www.youtube.com/watch?v		
Initiating Fluency with Addition and Subtraction within 100	Lesson 4	Make a ten to add and subtract within 20. https://www.youtube.com/watch?v		
	Lesson 5	Decompose a number into a ten and some ones and subtract from that ten when subtracting within 20 and apply to one-step word problems. <u>https://www.youtube.com/watch?v</u>		
	Lesson 6	Add and subtract within multiples of ten based on understanding place value and basic facts. https://www.youtube.com/watch?v		
	Lesson 7	Add within 100 using properties of addition to make a ten. https://www.youtube.com/watch?v		
	Lesson 8	Decompose to subtract from a ten when subtracting within 100 and apply to one-step word problems. <u>https://www.youtube.com/watch?v</u>		
	Er	nd-of- Module Assessment		

Modifications			
Special Education/ 504:	English Language Learners:		
 -Adhere to all modifications and health concerns stated in each IEP. -Give students a Menu, allowing students to pick assignments from different levels based on difficulty. -Accommodate Instructional Strategies: reading aloud text, graphic organizers, one-on-one instruction, class website (Google Classroom), handouts, definition list with visuals, extended time -Allow students to demonstrate understanding of a problem by drawing the picture of the answer and then explaining the reasoning orally and/or in writing, such as Read-Draw-Write -Provide breaks between tasks, use positive reinforcement, use proximity -Assure students have experiences that are on the Concrete- Pictorial- Abstract spectrum by using manipulatives -Common Core Approach to Differentiate Instruction: Students with Disabilities (pg 17-18) -Strategies for Students with 504 Plans 	 Use manipulatives to promote conceptual understanding and enhance vocabulary usage Provide graphic representations, gestures, drawings, equations, realia, and pictures during all segments of instruction During i-Ready lessons, click on "Español" to hear specific words in Spanish Utilize graphic organizers which are concrete, pictorial ways of constructing knowledge and organizing information Use sentence frames and questioning strategies so that students will explain their thinking/ process of how to solve word problems Utilize program translations (if available) for L1/ L2 students Reword questions in simpler language Make use of the ELL Mathematical Language Routines (click here for additional information) Scaffolding instruction for ELL Learners Common Core Approach to Differentiate Instruction: Students with Disabilities (pg 16-17) 		
Gifted and Talented:	Students at Risk for Failure:		
 Elevated contextual complexity Inquiry based or open ended assignments and projects More time to study concepts with greater depth Promote the synthesis of concepts and making real world connections Provide students with enrichment practice that are imbedded in the curriculum such as: Application / Conceptual Development Are you ready for more? Common Core Approach to Differentiate Instruction: Students with Disabilities (pg. 20) Provide opportunities for math competitions Alternative instruction pathways available 	 Assure students have experiences that are on the Concrete- Pictorial- Abstract spectrum Modify Instructional Strategies, reading aloud text, graphic organizers, one-on-one instruction, class website (Google Classroom), inclusion of more visu- als and manipulatives, Field Trips, Google Expedi- tions, Peer Support, one on one instruction Assure constant parental/ guardian contact through- out the year with successes/ challenges Provide academic contracts to students and guardi- ans Create an interactive notebook with samples, key vocabulary words, student goals/ objectives. Always plan to address students at risk in your learning tasks, instructions, and directions. Try to an- ticipate where the needs will be and then address them prior to lessons. Common Core Approach to Differentiate Instruc- tion: Students with Disabilities (pg 19) 		

21st Century Life and Career Skills:

Career Ready Practices describe the career-ready skills that all educators in all content areas should seek to develop in their students. They are practices that have been linked to increase college, career, and life success. Career Ready Practices should be taught and reinforced in all career exploration and preparation programs with increasingly higher levels of complexity and expectation as a student advances through a program of

study.

https://www.state.nj.us/education/cccs/2014/career/9.pdf

 CRP1. Act as a responsible and contributing citizen and employee. CRP2. Apply appropriate academic and technical skills. CRP3. Attend to personal health and financial well-being. CRP4. Communicate clearly and effectively and with reason. CRP5. Consider the environmental, social and economic impacts of decisions. CRP6. Demonstrate creativity and innovation. 	 CRP7. Employ valid and reliable research strategies. CRP8. Utilize critical thinking to make sense of problems and persevere in solving them. CRP9. Model integrity, ethical leadership and effective management. CRP10. Plan education and career paths aligned to personal goals. CRP11. Use technology to enhance productivity. CRP12. Work productively in teams while using cultural global competence. 		
Students are given an opportunity to communicate with peers effectively, clearly, and with the use of technical language. They are encouraged to reason through experiences that promote critical thinking and emphasize the importance of perseverance. Students are exposed to various mediums of technology, such as digital learning, calculators, and educational websites.			

Technology Standards:

All students will be prepared to meet the challenge of a dynamic global society in which they participate, contribute, achieve, and flourish through universal access to people, information, and ideas. https://www.state.nj.us/education/cccs/2014/tech/

8.1 Educational Technology:

All students will use digital tools to access, manage, evaluate, and synthesize information in order to solve problems individually and collaborate and to create and communicate knowledge.

- A. **Technology Operations and Concepts:** Students demonstrate a sound understanding of technology concepts, systems and operations.
- B. Creativity and Innovation: Students demonstrate creative thinking, construct knowledge and develop innovative products and process using technology.
- C. Communication and Collaboration: Students use digital media and environments to communicate and work collaboratively, including at a distance, to support individual learning and contribute to the learning of others.
- D. **Digital Citizenship:** Students understand human, cultural, and societal issues related to technology and practice legal and ethical behavior.
- E. **Research and Information Fluency:** Students apply digital tools to gather, evaluate, and use of information.
- F. Critical thinking, problem solving, and decision making: Students use critical thinking skills to plan and conduct research, manage projects, solve problems, and make informed decisions using appropriate digital tools and resources.

8.2 Technology Education, Engineering, Design, and Computational Thinking -Programming:

All students will develop an understanding of the nature and impact of technology, engineering, technological design, computational thinking and the designed world as they relate to the individual, global society, and the environment.

- A. The Nature of Technology: Creativity and Innovation- Technology systems impact every aspect of the world in which we live.
- B. **Technology and Society:** Knowledge and understanding of human, cultural, and societal values are fundamental when designing technological systems and products in the global society.
- C. **Design:** The design process is a systematic approach to solving problems.
- D. **Abilities in a Technological World:** The designed world in a product of a design process that provides the means to convert resources into products and systems.
- E. **Computational Thinking: Programming-**Computational thinking builds and enhances problem solving, allowing students to move beyond using knowledge to creating knowledge.

Interdisciplinary Connections:		
English Language Arts:		
RF.2.4	Read with sufficient accuracy and fluency to support comprehension.	
SL.2.1	Participate in collaborative conversations with diverse partners about <i>grade 2 topics and texts</i> with peers and adults in small and larger groups.	
L.2.4	Determine or clarify the meaning of unknown and multiple-meaning words and phrases based on grade 2 reading and content, choosing flexibly from an array of strategies.	

NJSLS Unpacked Standards		
<mark>2.0A.1</mark>	Use addition and subtraction within 100 to solve one- and two-step word problems involving sit- uations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem. ¹	
	•	
	¹ See Glossary, Table.	

Second Grade students extend their work with addition and subtraction word problems in two major ways. First, they represent and solve word problems within 100, building upon their previous work to 20. In addition, they represent and solve one and two-step word problems of all three types (Result Unknown, Change Unknown, Start Unknown). Please see **Table 1** at end of document for examples of all problem types.

One-step word problems use one operation. Two-step word problems use two operations which may include the same operation or opposite operations.

One Step Word Problem	Two-Step Word Problem	Two-Step Word Problem
One Operation	Two Operations, Same	Two Operations, Opposite
There are 15 stickers on the page.	There are 9 blue marbles and 6	There are 9 peas on the plate.
Brittany put some more stickers on	red marbles in the bag. Maria put	Carlos ate 5 peas. Mother put 7
the page. There are now 22 stickers	in 8 more marbles. How many	more peas on the plate. How
on the page. How many stickers did	marbles are in the bag now?	many peas are on the plate now?
Brittany put on the page?		
	9 + 6 + 8 = 🗖	9 –5 + 7 = 🗖
15 + 🗖 = 22		
22 – 15 = 🗖		

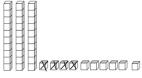
<u>Two-Step Problems</u>: Because Second Graders are still developing proficiency with the most difficult subtypes (shaded in white in Table 1 at end of the glossary): *Add To/Start Unknown; Take From/Start Unknown; Compare/Bigger Unknown; and Compare/Smaller Unknown,* two-step problems do **not** involve these sub-types (Common Core Standards Writing Team, May 2011). Furthermore, most two-step problems should focus on single-digit addends since the primary focus of the standard is the problem-type.

As second grade students solve one- and two-step problems they use manipulatives such as snap cubes, place value materials (groupable and pre-grouped), ten frames, etc.; create drawings of manipulatives to show their thinking; or use number lines to solve and describe their strategies. They then relate their drawings and materials to equations. By solving a variety of addition and subtraction word problems, second grade students determine the unknown in all positions (*Result* unknown, *Change* unknown, and *Start* unknown). Rather than a letter ("n"), boxes or pictures are used to represent the unknown number.

For example:					
Problem Type: Add To					
	<u>Result Unknown:</u>	<u>Change</u> Unknown:	<u>Start Unknown:</u>		
	There are 29 students on	There are 29 students on the	There are some students on the		
	the playground. Then 18	playground. Some more stu-	playground. Then 18 more students		
	more students showed up.	dents show up. There are	came. There are now 47 students.		
	How many students are	now 47 students. How many	How many students were on the		
	there now?	students came?	playground at the beginning?		
	29 + 18 = 🗖	29 + 💭 = 47	□ + 18 = 47		
Second Gra	iders use a range of methods, o	ften mastering more complex st	rategies such as making tens and double	es and near	
doubles fo	r problems involving addition a	nd subtraction within 20. Movin	g beyond counting and counting-on, see	ond grade	
	students apply	y their understanding of place va	lue to solve problems.		
One-Step Ex	ample: Some students are in t	he cafeteria. 24 more students	came in. Now there are 60 students in	the cafete-	
	ria. How many were in the caf	eteria to start with? Use drawin	gs and equations to show your thinking		
Student A:	I read the equation and though	it about how to write it with nun	nbers. I thought, "What and 24 makes 6	50?" So, my	
	equation for the	oroblem is 🛛 + 24 = 60. I used	l a number line to solve it.		
I started wi	I started with 24. Then I took jumps of 10 until I got close to 60. I landed on 54. Then, I took a jump of 6 to get to 60. So, 10 +				
	10 + 10 + 6 = 36.	So, there were 36 students in the	ne cafeteria to start with.		
10 10 10 6					
24 34 44 54 60					
Student B: I read the equation and thought about how to write it with numbers. I thought, "There are 60 total. I know about					
the 24. So, what is 60 – 24?" So, my equation for the problem is $60 - 24 = \Box$ I used place value blocks to solve it.					
I started with 60 and took 2 tens away.					

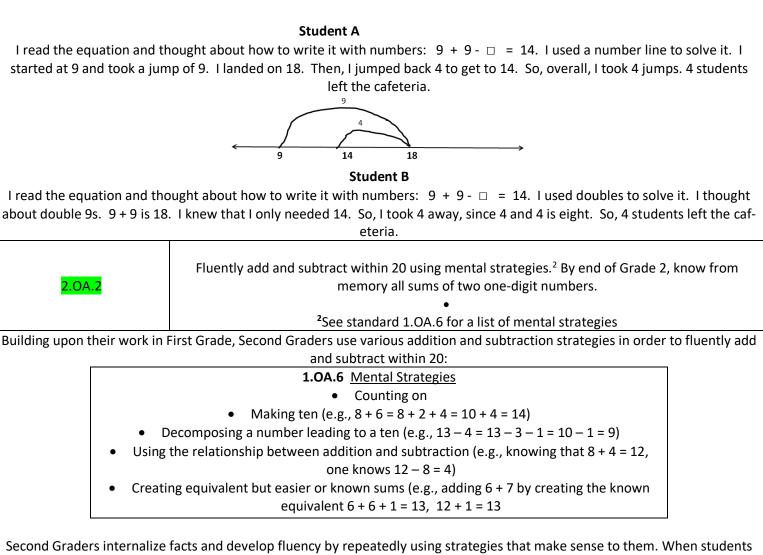


I needed to take 4 more away. So, I broke up a ten into ten ones. Then, I took 4 away.



That left me with 36. So, 36 students were in the cafeteria at the beginning. 60 - 24 = 36

<u>Two-Step Example</u>: There are 9 students in the cafeteria. 9 more students come in. After a few minutes, some students leave. There are now 14 students in the cafeteria. How many students left the cafeteria? Use drawings and equations to show your thinking.



Second Graders internalize facts and develop fluency by repeatedly using strategies that make sense to them. When students are able to demonstrate fluency they are accurate, efficient, and flexible. Students must have efficient strategies in order to know sums from memory.

Research indicates that teachers can best support students' memory of the sums of two one-digit numbers through varied experiences including making 10, breaking numbers apart, and working on mental strategies. These strategies replace the use of repetitive timed tests in which students try to memorize operations as if there were not any relationships among the various facts. When teachers teach facts for automaticity, rather than memorization, they encourage students to think about the relationships among the facts. (Fosnot & Dolk, 2001)

It is no accident that the standard says "know from memory" rather than "memorize". The first describes an outcome, whereas the second might be seen as describing a method of achieving that outcome. So no, the standards are not dictating timed tests. (McCallum, October 2011)

Developing Fluency for Addition & Subtraction within 20 <u>Example</u>: **9 + 5=** ___

Student A Counting On

I started at 9 and then counted 5 more. I landed on 14. **Student B** Decomposing a Number-Leading to a Ten

I know that 9 and 1 is 10, so I broke 5 into 1 and 4. 9 plus 1 is 10. Then I have to add 4 more, which is 14.

Example: **13 - 9 =**

Student A Using the Relationship between Addition and Subtraction

I know that 9 plus 4 equals 13. So 13 minus 9 is 4.

Student B Creating an Easier Problem

Instead of 13 minus 9, I added 1 to each of the numbers to make the problem 14 minus 10. I know the answer is 4. So 13 minus 9 is also 4.

Common addition and subtraction.¹

	RESULT UNKNOWN	CHANGE UNKNOWN	START UNKNOWN
	Two bunnies sat on the grass.	Two bunnies were sitting on	Some bunnies were sitting on
ADD TO	Three more bunnies hopped	the grass. Some more bunnies	the grass. Three more bunnies
	there. How many bunnies are	hopped there. Then there were	hopped there. Then there we
ADD TO	on the grass now? 2+3=?	five bunnies. How many	five bunnies. How many
		bunnies hopped over to the	bunnies were on the grass
		first two? 2 + ? = 5	before??+3=5
	Five apples were on the table. I	Five apples were on the table. I	Some apples were on the tabl
	ate two apples. How many	ate some apples. Then there	I ate two apples. Then there
TAKE FROM	apples are on the table now?5-	were three apples. How many	were three apples. How many
	2 = ?	apples did I eat?5 - ? = 3	apples were on the table
			before??-2 = 3
	TOTAL UNKNOWN	ADDEND UNKNOWN	BOTH ADDENDS
			UNKNOWN ²
	Three red apples and two green	Five apples are on the table.	Grandma has five flowers. Ho
	apples are on the table. How	Three are red and the rest are	many can she put in the red
PUT TOGETHER / TAKE APART ³	many apples are on the table? 3	green. How many apples are	vase and how many in her blu
IAKE APART *	+ 2 = ?	green? 3+?=5,5-3=?	vase? 5 = 0 + 5, 5 + 0 5 = 1 + 4
			= 4 + 1, 5 = 2 + 3, 5 = 3 + 2
COMPARE	DIFFERENCE UKNOWN	BIGGER UNKNOWN	= 4+1, 5 = 2 + 3, 5 = 3 + 2 SMALLER UNKNOWN
COMPARE	DIFFERENCE UKNOWN ("How many more?"	BIGGER UNKNOWN (Version with "more"): Julie has	SMALLER UNKNOWN
COMPARE			SMALLER UNKNOWN (Version with "more"): Julie ha
COMPARE	("How many more?"	(Version with "more"): Julie has	SMALLER UNKNOWN (Version with "more"): Julie ha three more apples than Lucy.
COMPARE	("How many more?" version):Lucy has two apples.	(Version with "more"): Julie has three more apples than	SMALLER UNKNOWN (Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How man
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How	SMALLER UNKNOWN (Version with "more"): Julie ha three more apples than Lucy. Julie has five apples. How man apples does Lucy have?(Version
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have?	SMALLER UNKNOWN (Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How man apples does Lucy have?(Versio with "fewer"): Lucy has 3 fewe
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy?("How many fewer?"	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have? (Version with "fewer"): Lucy has	SMALLER UNKNOWN (Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How man apples does Lucy have?(Version with "fewer"): Lucy has 3 fewe apples than Julie. Julie has five
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy?("How many fewer?" version): Lucy has two apples. Julie has five apples. How many fewer apples does Lucy have	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have? (Version with "fewer"): Lucy has 3 fewer apples than Julie. Lucy	SMALLER UNKNOWN (Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How man apples does Lucy have?(Version with "fewer"): Lucy has 3 fewer apples than Julie. Julie has five apples. How many apples does
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy?("How many fewer?" version): Lucy has two apples. Julie has five apples. How many	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have? (Version with "fewer"): Lucy has 3 fewer apples than Julie. Lucy has two apples. How many	• •

¹ Adapted from Box 2-4 of Mathematics Learning in Early Childhood, National Research Council (2009, pp. 32, 33).

² These take apart situations can be used to show all the decompositions of a given number. The associated equations, which have the total on the left of the equal sign, help children understand that the – sign does not always mean, makes or results in but always does mean is the same number as.

³ Either addend can be unknown, so there are three variations of these problem situations. Both addends Unknown is a productive extension of the basic situation, especially for small numbers less than or equal to 10.

⁴ For the Bigger Unknown or Smaller Unknown situations, one version directs the correct operation (the version using more for the bigger unknown and using less for the smaller unknown). The other versions are more difficult.

http://www.corestandards.org/Math/Content/mathematics-glossary/Table-1/

Module 1 Assessment Framework				
Assessment NJSLS Estimated Time Format				
Diagnostic Assessment 1 (iReady)		1-2 blocks	Individual	
Optional End-of- Module Assessment (Interview Style)	2.OA.1-2 2.NBT.5	1 Block	Individual or Small Group with Teacher	

Module 1 Performance Assessment/ PBL Framework			
Assessment	NJSLS	Estimated Time	Format
Module 1 Performance Task 1 <i>Peanuts and Ducks</i>	2.NBT.5	Up to 30 minutes	Individual or Small Group
Extended Constructed Response (ECR)* (click here for access)	Dependent on unit of study & month of administration	Up to 30 Minutes	Individual

Use the following links to access ECR protocol and district assessment scoring documents:

- Assessment and Data in Mathematics Bulletin
- ECR Protocol

Second Grade Unit 1: Sums/ Differences to 20

Second Grade Ideal Math Block

Fluency: Whole Group Sprints, Counting, Whiteboard Exchange				
N work to allow children new MA Technology Integration:	to ACT OUT or ENGAG TH IDEA <u>https://embarc.online</u>	E ACTIVELY with the		-
Concept Development: Individual/partner/whole Instruction & Strategic Problem Set Questions Technology Integration: <u>https://embarc.online/</u> Website provides Goggle slides, additional activities, and student videos. per lesson				50-60 min.
Student Debrief: Whole Group Exit Ticket: Independent				
Pairs / Small Gr activities designed to RE	OUD/ INDIVIDUA TEACH, REMEDIATE, E			
A: Application/ Problem Solving	T: Technology Resources I-ready Zearn	H: Hands on Activities		20-30 min.
	Sprints, Counting, W pplication Proble N work to allow children new MA Technology Integration: Goggle slides, addition Struction & Strategic echnology Integration is Goggle slides, additi les Student Debrie Exit Ticket: I CENTERS/ Pairs / Small Gr activities designed to RE derstanding A: Application/ Problem	Sprints, Counting, Whiteboard Exchange pplication Problem: Whole Group N work to allow children to ACT OUT or ENGAGE new MATH IDEA Technology Integration: https://embarc.online Goggle slides, additional activities, and studer Development: Individual/partr nstruction & Strategic Problem Set Questic echnology Integration: https://embarc.online is Goggle slides, additional activities, and st lesson Student Debrief: Whole Group Exit Ticket: Independent CENTERS/STATIONS: Pairs / Small Group/ Individua activities designed to RETEACH, REMEDIATE, E derstanding of concepts. A: Application/ Problem Solving Technology Resources I-ready	Sprints, Counting, Whiteboard Exchange plication Problem: Whole Group work to allow children to ACT OUT or ENGAGE ACTIVELY with the new MATH IDEA Technology Integration: https://embarc.online/ to coggle slides, additional activities, and student videos per lesson prouction & Strategic Problem Set Questions echnology Integration: https://embarc.online/ to coggle slides, additional activities, and student videos. per lesson Student Debrief: Whole Group Exit Ticket: Independent CENTERS/STATIONS: Pairs / Small Group/ Individual activities designed to RETEACH, REMEDIATE, ENRICH student's un- derstanding of concepts. A: A: A: A: A: A: A: A: A: A:	Sprints, Counting, Whiteboard Exchange plication Problem: Whole Group work to allow children to ACT OUT or ENGAGE ACTIVELY with the new MATH IDEA Technology Integration: https://embarc.online/ coggle slides, additional activities, and student videos per lesson problem Strategic Problem Set Questions actionology Integration: https://embarc.online/ soggle slides, additional activities, and student videos.per lesson stuction & Strategic Problem Set Questions activities, additional activities, and student videos.per lesson student Debrief: Whole Group Exit Ticket: Independent Exit Ticket: Independent Activities designed to RETEACH, REMEDIATE, ENRICH student's un- derstanding of concepts. A: A: A: A: A: A: A: A: A: B: A: A: A: B: B: B: B: B: B: B: B: B: B

Lesson Structure:

Fluency:

- Sprints
- Whiteboard Exchange

Technology Integration:

Splat Sequences

Which one doesn't belong?

Would you rather?

Esti- Mysteries

Anchor Task:

- Engage students in using the RDW Process
- Sequence problems from simple to complex and adjust based on students' responses
- Facilitate share and critique of various explanations, representations, and/or examples.

Guided Practice/ Independent Practice : (largest chunk of time)

Instruction:

- Maintain overall alignment with the objectives and suggested pacing and structure.
- Use of tools, precise mathematical language, and/or models
- Balance teacher talk with opportunities for peer share and/or collaboration
- Generate next steps by watching and listening for understanding

Problem Set: (Individual, partner, or group)

- Allow for independent practice and productive struggle
- Assign problems strategically to differentiate practice as needed
- Create and assign remedial sequences as needed

Technology Integration:

- Think Central:
 - Pre-Test
 - Chapter Review
 - Test Prep
 - Performance Tasks

https://embarc.online/

Virtual Manipulatives for lessons

http://nlvm.usu.edu/en/nav/vlibrary.html

For videos that students can watch and interact with independently click here

Student Debrief:

- Elicit students thinking, prompt reflection, and promote metacognition through student centered discussion
- Culminate with students' verbal articulation of their learning for the day
- Close with completion of the daily Exit Ticket (opportunity for informal assessment that guides effective preparation of subsequent lessons) as needed.

Centers:

- I-Ready: <u>https://login.i-ready.com/</u> *i-Ready* makes the promise of differentiated instruction a practical reality for teachers and students. It was designed to get students excited about learning and to support teachers in the challenge of meeting the needs of all learners. Through the power of one intuitive system whose pieces were built from the ground up to work together, teachers have the tools they need to ensure students are on the road to proficiency.
- Zearn: <u>https://www.zearn.org/</u>Zearn Math is a K-5 math curriculum based on Eureka Math with top-rated materials for teacher-led and digital instruction.
- Teacher Toolbox; <u>https://teacher-toolbox.com/</u> A digital collection of K-8 resources to help you differentiate instruction to students performing on, below, and above grade level.

NJSLA Assessment Evidence/Clarification Statements			
NJSLS	Evidence Statement	Clarification	Math Practices
2.NBT.5	Fluently add and subtract within 100 us- ing strategies based on place value, properties of operations, and/or the rela- tionship between addition and subtrac- tion.	 Tasks do not have a context. Sums and differences beyond 20 but within 100 should be emphasized in 75% of the tasks. Only the answer is required (strategies, representations, etc. are not assessed here). 	MP 7,8
2.0A.1-1	Use addition and subtraction within 100 to solve one- step word problems involv- ing situations of adding to, taking from, putting together, taking apart, and com- paring, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.	 All problem situations and all of their subtypes and language variants are included but 40% of tasks should include the most difficult problem subtypes and language variants. Addition and subtraction is emphasized beyond 20 but within 100 For more information see CCSS Table 1, p. 88 and the OA Progression 	MP 1, 4
2.0A.1-2	Use addition and subtraction within 100 to solve two- step word problems involv- ing situations of adding to, taking from, putting together, taking apart, and com- paring, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.	 The majority of problems (75%) involve single-digit addends. The most difficult problem subtypes and language variants should not be included in these problems. For more information see CCSS Table 1, p. 88 and the OA Progression. 	MP 1, 4
2.OA.2	Fluently add and subtract within 20 using mental strategies. By end of Grade 2, know from memory all sums of two one- digit numbers.	 Tasks do not have a context. Only the answer is required (strate-gies, representations, etc. are not assessed here). Tasks require fluent (fast and accurate) finding of sums and related differences. 	

Number Talks

What does Number Talks look like?

- Students are near each other so they can communicate with each other (central meeting place)
- Students are mentally solving problems
- Students are given thinking time
- Thumbs up show when they are ready
- Teacher is recording students' thinking

Communication

- Having to talk out loud about a problem helps students clarify their own thinking
- Allow students to listen to other's strategies and value other's thinking
- Gives the teacher the opportunity to hear student's thinking

Mental Math

- When you are solving a problem mentally you must rely on what you know and understand about the numbers instead of memorized procedures
- You must be efficient when computing mentally because you can hold a lot of quantities in your head

Thumbs Up

- This is just a signal to let you know that you have given your students enough time to think about the problem
- If will give you a picture of who is able to compute mentally and who is struggling
- It isn't as distracting as a waving hand

Teacher as Recorder

- Allows you to record students' thinking in the correct notation
- Provides a visual to look at and refer back to
- Allows you to keep a record of the problems posed and which students offered specific strategies

Purposeful Problems

- Start with small numbers so the students can learn to focus on the strategies instead of getting lost in the numbers
- Use a number string (a string of problems that are related to and scaffold each other)

Starting Number Talks in your Classroom

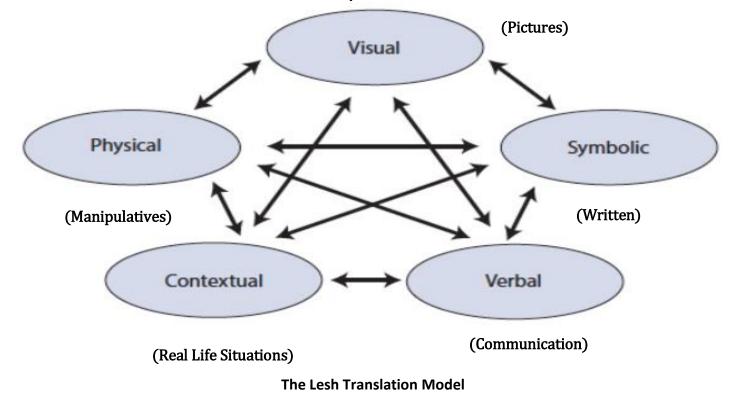
- Start with specific problems in mind
- Be prepared to offer a strategy from a previous student
- It is ok to put a student's strategy on the backburner
- Limit your number talks to about 15 minutes
- Ask a question, don't tell!

The teacher asks questions:

- Who would like to share their thinking?
- Who did it another way?
- How many people solved it the same way as Billy?
- Does anyone have any questions for Billy?
- Billy, can you tell us where you got that 5?

Second Grade Unit 1: Sums/ Differences to 20

Student Name: Date:	Task: School: Teacher:				
	STUDENT FRIENDLY RUBRIC			SCORE	
"I CAN"	a start 1	getting there 2	that's it 3	WOW! 4	SCORE
Understand	l need help.	I need some help.	l do not need help.	I can help a class- mate.	
Solve	I am unable to use a strategy.	I can start to use a strategy.	I can solve it more than one way.	I can use more than one strategy and talk about how they get to the same answer.	
Say or Write	l am unable to say or write.	l can write or say some of what I did.	I can write and talk about what I did. I can write or talk about why I did it.	I can write and say what I did and why I did it.	
Draw or Show	I am not able to draw or show my thinking.	I can draw, but not show my thinking; or I can show but not draw my thinking;	I can draw and show my thinking	I can draw, show and talk about my think- ing.	



Use and Connection of Mathematical Representations

Each oval in the model corresponds to one way to represent a mathematical idea.

Visual: When children draw pictures, the teacher can learn more about what they understand about a particular mathematical idea and can use the different pictures that children create to provoke a discussion about mathematical ideas. Constructing their own pictures can be a powerful learning experience for children because they must consider several aspects of mathematical ideas that are often assumed when pictures are pre-drawn for students.

Physical: The manipulatives representation refers to the unifix cubes, base-ten blocks, fraction circles, and the like, that a child might use to solve a problem. Because children can physically manipulate these objects, when used appropriately, they provide opportunities to compare relative sizes of objects, to identify patterns, as well as to put together representations of numbers in multiple ways.

Second Grade Unit 1: Sums/ Differences to 20

Verbal: Traditionally, teachers often used the spoken language of mathematics but rarely gave students opportunities to grapple with it. Yet, when students do have opportunities to express their mathematical reasoning aloud, they may be able to make explicit some knowledge that was previously implicit for them.

Symbolic: Written symbols refer to both the mathematical symbols and the written words that are associated with them. For students, written symbols tend to be more abstract than the other representations. I tend to introduce symbols after students have had opportunities to make connections among the other representations, so that the students have multiple ways to connect the symbols to mathematical ideas, thus increasing the likelihood that the symbols will be comprehensible to students.

Contextual: A relevant situation can be any context that involves appropriate mathematical ideas and holds interest for children; it is often, but not necessarily, connected to a real-life situation.

The Lesh Translation Model: Importance of Connections

As important as the ovals are in this model, another feature of the model is even more important than the representations themselves: The arrows! The arrows are important because they represent the connections students make between the representations. When students make these connections, they may be better able to access information about a mathematical idea, because they have multiple ways to represent it and, thus, many points of access.

Individuals enhance or modify their knowledge by building on what they already know, so the greater the number of representations with which students have opportunities to engage, the more likely the teacher is to tap into a student's prior knowledge. This "tapping in" can then be used to connect students' experiences to those representations that are more abstract in nature (such as written symbols). Not all students have the same set of prior experiences and knowledge. Teachers can introduce multiple representations in a meaning-ful way so that students' opportunities to grapple with mathematical ideas are greater than if their teachers used only one or two representations.

Concrete Pictorial Abstract (CPA) Instructional Approach

The CPA approach suggests that there are three steps necessary for pupils to develop understanding of a mathematical concept.

Concrete: "Doing Stage": Physical manipulation of objects to solve math problems.
Pictorial: "Seeing Stage": Use of imaged to represent objects when solving math problems.
Abstract: "Symbolic Stage": Use of only numbers and symbols to solve math problems.

CPA is a gradual systematic approach. Each stage builds on to the previous stage. Reinforcement of concepts are achieved by going back and forth between these representations and making connections between stages. Students will benefit from seeing parallel samples of each stage and how they transition from one to another.

Read, Draw, Write Process

READ the problem. Read it over and over.... And then read it again.

DRAW a picture that represents the information given. During this step students ask themselves: Can I draw something from this information? What can I draw? What is the best model to show the information? What conclusions can I make from the drawing?

WRITE your conclusions based on the drawings. This can be in the form of a number sentence, an equation, or a statement.

Students are able to draw a model of what they are reading to help them understand the problem. Drawing a model helps students see which operation or operations are needed, what patterns might arise, and which models work and do not work. Students must dive deeper into the problem by drawing models and determining which models are appropriate for the situation.

While students are employing the RDW process they are using several Standards for Mathematical Practice and in some cases, all of them.

Mathematical Discourse and Strategic Questioning

Discourse involves asking strategic questions that elicit from students their understanding of the context and actions taking place in a problem, how a problem is solved and why a particular method was chosen. Students learn to critique their own and others' ideas and seek out efficient mathematical solutions.

While classroom discussions are nothing new, the theory behind classroom discourse stems from constructivist views of learning where knowledge is created internally through interaction with the environment. It also fits in with sociocultural views on learning where students working together are able to reach new understandings that could not be achieved if they were working alone.

Underlying the use of discourse in the mathematics classroom is the idea that mathematics is primarily about reasoning not memorization. Mathematics is not about remembering and applying a set of procedures but about developing understanding and explaining the processes used to arrive at solutions.

Teacher Questioning:

Asking better questions can open new doors for students, promoting mathematical thinking and classroom discourse. Can the questions you're asking in the mathematics classroom be answered with a simple "yes" or "no," or do they invite students to deepen their understanding?



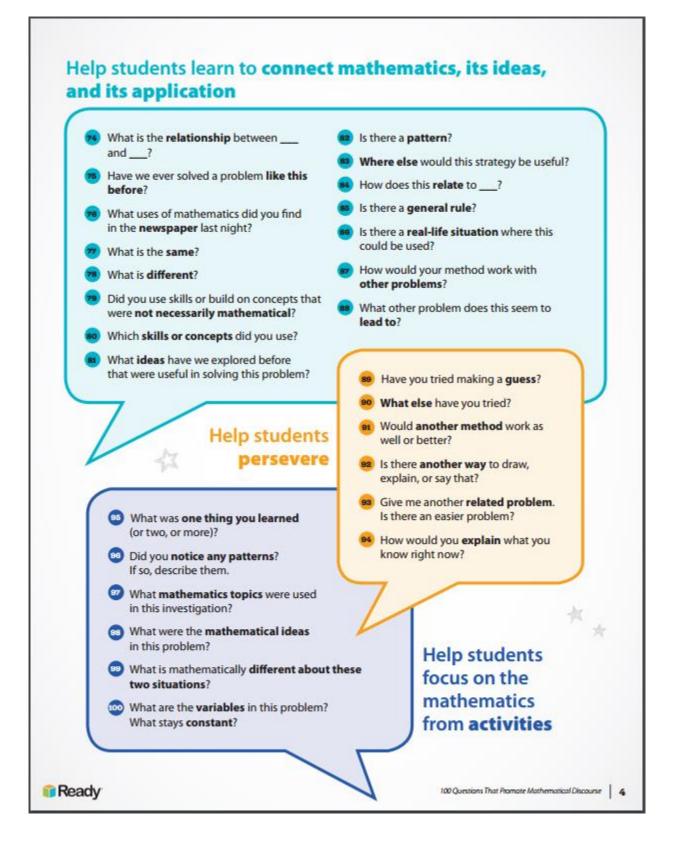
Albert Einstein

To help you encourage deeper discussions, here are 100 questions to incorporate into your instruction by Gladis Kersaint, mathematics expert and advisor for Ready Mathematics.

Disco	ematical
 What strategy did you use? Do you agree? Do you disagree? Would you ask the rest of the class that question? Could you share your method with the class? What part of what he said do you understand? Would someone like to share? Can you convince the rest of us the your answer makes sense? What do others think about what [student] said? 	 Have you discussed this with your group? With others? Did anyone get a different answer? Where would you go for help? Did everybody get a fair chance to talk, use the manipulatives, or be the recorder? How could you help another student without telling them the answer?
Help students rely more on themselves to determine whether something is mathematically correct	 Is this a reasonable answer? Does that make sense? Why do you think that? Why is that true? Can you draw a picture or make a model to show that? How did you reach that conclusion? Does anyone want to revise his or her answer? How were you sure your answer was right?







Conceptual Understanding

Students demonstrate conceptual understanding in mathematics when they provide evidence that they can:

- recognize, label, and generate examples of concepts;
- use and interrelate models, diagrams, manipulatives, and varied representations of concepts;
- identify and apply principles; know and apply facts and definitions;
- compare, contrast, and integrate related concepts and principles; and
- recognize, interpret, and apply the signs, symbols, and terms used to represent concepts.

Conceptual understanding reflects a student's ability to reason in settings involving the careful application of concept definitions, relations, or representations of either.

Procedural Fluency

Procedural fluency is the ability to:

- apply procedures accurately, efficiently, and flexibly;
- to transfer procedures to different problems and contexts;
- to build or modify procedures from other procedures; and
- to recognize when one strategy or procedure is more appropriate to apply than another.

Procedural fluency is more than memorizing facts or procedures, and it is more than understanding and being able to use one procedure for a given situation. Procedural fluency builds on a foundation of conceptual understanding, strategic reasoning, and problem solving (NGA Center & CCSSO, 2010; NCTM, 2000, 2014). Research suggests that once students have memorized and practiced procedures that they do not understand, they have less motivation to understand their meaning or the reasoning behind them (Hiebert, 1999). Therefore, the development of students' conceptual understanding of procedures should precede and coincide with instruction on procedures.

Math Fact Fluency: Automaticity

Students who possess math fact fluency can recall math facts with automaticity. Automaticity is the ability to do things without occupying the <u>mind</u> with the low-level details required, allowing it to become an automatic response pattern or <u>habit</u>. It is usually the result of <u>learning</u>, <u>repetition</u>, and practice.

K-2 Math Fact Fluency Expectation

K.OA.5 Add and Subtract within 5.1.OA.6 Add and Subtract within 10.2.OA.2 Add and Subtract within 20.

Math Fact Fluency: Fluent Use of Mathematical Strategies

First and second grade students are expected to solve addition and subtraction facts using a variety of strategies fluently.

1.OA.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as:

- counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14);
- decomposing a number leading to a ten (e.g., 13 4 = 13 3 1 = 10 1 = 9);
- using the relationship between addition and subtraction; and
- creating equivalent but easier or known sums.

2.NBT.7 Add and subtract within 1000, using concrete models or drawings and strategies based on:

- o place value,
- o properties of operations, and/or
- \circ the relationship between addition and subtraction;

Evidence of Student Thinking

Effective classroom instruction and more importantly, improving student performance, can be accomplished when educators know how to elicit evidence of students' understanding on a daily basis. Informal and formal methods of collecting evidence of student understanding enable educators to make positive instructional changes. An educators' ability to understand the processes that students use helps them to adapt instruction allowing for student exposure to a multitude of instructional approaches, resulting in higher achievement. By highlighting student thinking and misconceptions, and eliciting information from more students, all teachers can collect more representative evidence and can therefore better plan instruction based on the current understanding of the entire class.

Mathematical Proficiency

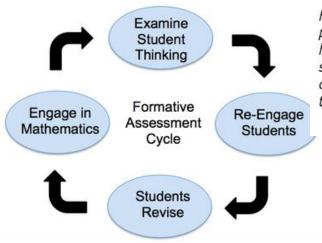
To be mathematically proficient, a student must have:

- <u>Conceptual understanding</u>: comprehension of mathematical concepts, operations, and relations;
- <u>Procedural fluency</u>: skill in carrying out procedures flexibly, accurately, efficiently, and appropriately;
- <u>Strategic competence</u>: ability to formulate, represent, and solve mathematical problems;
- <u>Adaptive reasoning</u>: capacity for logical thought, reflection, explanation, and justification;
- Productive disposition: habitual inclination to see mathematics as sensible, useful, and worthwhile,

coupled with a belief in diligence and one's own efficacy.

Evidence should:

- Provide a window in student thinking;
- Help teachers to determine the extent to which students are reaching the math learning goals; and
- Be used to make instructional decisions during the lesson and to prepare for subsequent lessons.



Formative assessment is an essentially interactive process, in which the teacher can find out whether what has been taught has been learned, and if not, to do something about it. Day-to-day formative assessment is one of the most powerful ways of improving learning in the mathematics classroom.

(Wiliam 2007, pp. 1054; 1091)

Connections to the Mathematical Practices

Student Friendly Connections to the Mathematical Practices

- 1. I can solve problems without giving up.
- 2. I can think about numbers in many ways.
- 3. I can explain my thinking and try to understand others.
- 4. I can show my work in many ways.
- 5. I can use math tools and tell why I choose them.
- 6. I can work carefully and check my work.
- 7. I can use what I know to solve new problems.
- 8. I can discover and use short cuts.

The **Standards for Mathematical Practice** describe varieties of expertise that mathematics educators at all levels should seek to develop in their students.

Make sense of problems and persevere in solving them

In Kindergarten, students learn that doing math involves solving problems and discussing how they solved them. Students will begin to explain the meaning of a problem, and look for ways to solve it. Kindergarteners will learn how to use objects and pictures to help them understand and solve problems. They will begin to check their thinking when the teacher asks them how they got their answer, and if the answer makes sense. When working in small groups or with a partner they will listen to the strategies of the group and will try different approaches.

Reason abstractly and quantitatively

1

2

Mathematically proficient students in Kindergarten make sense of quantities and the relationships while solving tasks. This involves two processes- decontextualizing and contextualizing. In Kindergarten, students represent situations by decontextualizing tasks into numbers and symbols. For example, in the task, "There are 7 children on the playground and some children go line up. If there are 4 children still playing, how many children lined up?" Kindergarten students are expected to translate that situation into the equation: 7-4 =____, and then solve the task. Students also contextualize situations during the problem solving process. For example, while solving the task above, students refer to the context of the task to determine that they need to subtract 4 since the number of children on the playground is the total number of students except for the 4 that are still playing. Abstract reasoning also occurs when students measure and compare the lengths of objects.

Construct viable arguments and critique the reasoning of others

Mathematically proficient students in Kindergarten accurately use mathematical terms to construct arguments and engage in discussions about problem solving strategies. For example, while solving the task, "There are 8 books on the shelf. If you take some books off the shelf and there are now 3 left, how many books did you take off the shelf?" students will solve the task, and then be able to construct an accurate argument about why they subtracted 3 form

8 rather than adding 8 and 3. Further, Kindergarten students are expected to examine a variety of problem solving strategies and begin to recognize the reasonableness of them, as well as similarities and differences among them.

Model with mathematics

3

4

5

Mathematically proficient students in Kindergarten model real-life mathematical situations with a number sentence or an equation, and check to make sure that their equation accurately matches the problem context. Kindergarten students rely on concrete manipulatives and pictorial representations while solving tasks, but the expectation is that they will also write an equation to model problem situations. For example, while solving the task "there are 7 bananas on the counter. If you eat 3 bananas, how many are left?" Kindergarten students are expected to write the equation 7-3 = 4. Likewise, Kindergarten students are expected to create an appropriate problem situation from an equation. For example, students are expected to orally tell a story problem for the equation 4+5 = 9.

Use appropriate tools strategically

Mathematically proficient students in Kindergarten have access to and use tools appropriately. These tools may include counters, place value (base ten) blocks, hundreds number boards, number lines, and concrete geometric shapes (e.g., pattern blocks, 3-d solids). Students should also have experiences with educational technologies, such as calculators, virtual manipulatives, and mathematical games that support conceptual understanding. During classroom instruction, students should have access to various mathematical tools as well as paper, and determine which tools are the most appropriate to use. For example, while solving the task "There are 4 dogs in the park. If 3 more dogs show up, how many dogs are they?" Kindergarten students are expected to explain why they used specific mathematical tools."

Attend to precision

Mathematically proficient students in Kindergarten are precise in their communication, calculations, and measurements. In all mathematical tasks, students in Kindergarten describe their actions and strategies clearly, using gradelevel appropriate vocabulary accurately as well as giving precise explanations and reasoning regarding their process of finding solutions. For example, while measuring objects iteratively (repetitively), students check to make sure that there are no gaps or overlaps. During tasks involving number sense, students check their work to ensure the accuracy and reasonableness of solutions.

Look for and make use of structure

7

Mathematically proficient students in Kindergarten carefully look for patterns and structures in the number system and other areas of mathematics. While solving addition problems, students begin to recognize the commutative property, in that 1+4 = 5, and 4+1 = 5. While decomposing teen numbers, students realize that every number between 11 and 19, can be decomposed into 10 and some leftovers, such as 12 = 10+2, 13 = 10+3, etc. Further, Kindergarten students make use of structures of mathematical tasks when they begin to work with subtraction as missing addend problems, such as 5-1 =___ can be written as 1+__ = 5 and can be thought of as how much more do I need to add to 1 to get to 5?

Look for and express regularity in repeated reasoning

Mathematically proficient students in Kindergarten begin to look for regularity in problem structures when solving mathematical tasks. Likewise, students begin composing and decomposing numbers in different ways. For example, in the task "There are 8 crayons in the box. Some are red and some are blue. How many of each could there be?" Kindergarten students are expected to realize that the 8 crayons could include 4 of each color (4+4 = 8), 5 of one color and 3 of another (5+3 = 8), etc. For each solution, students repeated engage in the process of finding two numbers that can be joined to equal 8.

Effective Mathematics Teaching Practices

Establish mathematics goals to focus learning. Effective teaching of mathematics establishes clear goals for the mathematics that students are learning, situates goals within learning progressions, and uses the goals to guide instructional decisions.

Implement tasks that promote reasoning and problem solving. Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving and allow multiple entry points and varied solution strategies.

Use and connect mathematical representations. Effective teaching of mathematics engages students in making connections among mathematical representations to deepen understanding of mathematics concepts and procedures and as tools for problem solving.

Facilitate meaningful mathematical discourse. Effective teaching of mathematics facilitates discourse among students to build shared understanding of mathematical ideas by analyzing and comparing student approaches and arguments.

Pose purposeful questions. Effective teaching of mathematics uses purposeful questions to assess and advance students' reasoning and sense making about important mathematical ideas and relationships.

Build procedural fluency from conceptual understanding. Effective teaching of mathematics builds fluency with procedures on a foundation of conceptual understanding so that students, over time, become skillful in using procedures flexibly as they solve contextual and mathematical problems.

Support productive struggle in learning mathematics. Effective teaching of mathematics consistently provides students, individually and collectively, with opportunities and supports to engage in productive struggle as they grapple with mathematical ideas and relationships.

Elicit and use evidence of student thinking. Effective teaching of mathematics uses evidence of student thinking to assess progress toward mathematical understanding and to adjust instruction continually in ways that support and extend learning.

	5 Practices for Orchestrating Productive Mathematics Discussions
Practice	Description/ Questions
1. Anticipating	What strategies are students likely to use to approach or solve a challenging high-level mathematical task?
	How do you respond to the work that students are likely to produce?
	Which strategies from student work will be most useful in addressing the mathematical goals?
2. Monitoring	Paying attention to what and how students are thinking during the lesson.
	Students working in pairs or groups
	Listening to and making note of what students are discussing and the strategies they are using
	Asking students questions that will help them stay on track or help them think more deeply about the task. (Pr mote productive struggle)
3. Selecting	This is the process of deciding the <i>what</i> and the <i>who</i> to focus on during the discussion.
4. Sequencing	What order will the solutions be shared with the class?
5. Connecting	Asking the questions that will make the mathematics explicit and understandable.
	Focus must be on mathematical meaning and relationships; making links between mathematical ideas and rep sentations.

MATH CENTERS/ WORKSTATIONS

Math workstations allow students to engage in authentic and meaningful hands-on learning. They often last for several weeks, giving students time to reinforce or extend their prior instruction. Before students have an opportunity to use the materials in a station, introduce them to the whole class, several times. Once they have an understanding of the concept, the materials are then added to the work stations.

Station Organization and Management Sample

Teacher A has 12 containers labeled 1 to 12. The numbers correspond to the numbers on the rotation chart. She pairs students who can work well together, who have similar skills, and who need more practice on the same concepts or skills. Each day during math work stations, students use the center chart to see which box they will be using and who their partner will be. Everything they need for their station will be in their box. **Each station is differentiated**. If students need more practice and experience working on numbers 0 to 10, those will be the only numbers in their box. If they are ready to move on into the teens, then she will place higher number activities into the box for them to work with.



In the beginning there is a lot of prepping involved in gathering, creating, and organizing the work stations. However, once all of the initial work is complete, the stations are easy to manage. Many of her stations stay in rotation for three or four weeks to give students ample opportunity to master the skills and concepts.

Read *Math Work Stations* by Debbie Diller.

In her book, she leads you step-by-step through the process of implementing work stations.

MATH WORKSTATION INFORMATION CARD

th Workstation:		Time:	
LS.:			
ective(s): By the end of this tas	k, I will be able to:		
•			
•			
k(s):			
•			
•			
•	<u> </u>		
•			
Ticket:			
•			
•			

Μ	IATH WORKSTATION	SCHEDULE		Week of:	
DAY	Technology	Problem Solving Lab	Fluency	Math	Small Group In-
	Lab		Lab	Journal	struction
Mon.					
	Group	Group	Group	Group	BASED
Tues.					ON CURRENT OB-
	Group	Group	Group	Group	SERVATIONAL DA-
Wed.					ТА
	Group	Group	Group	Group	
Thurs.					
	Group	Group	Group	Group	
Fri.					
	Group	Group	Group	Group	

INSTRUCTIONAL GROUPING

	GROUP A		GROUP B
1		1	
2		2	
3		3	
4		4	
5		5	
6		6	
	GROUP C		GROUP D
1		1	
2		2	
3		3	
4		4	
5		5	

Second Grade PLD Rubric

Got It			Not There Yet		
Evidence shows that the student essentially has the target concept		Student shows evidence of a major misunderstanding, incorrect concepts or procedure, or a failure to			
or big math idea.		engage in the task.			
PLD Level 5: 100%	PLD Level 4: 89%	PLD Level 3: 79%	PLD Level 2: 69%	PLD Level 1: 59%	
Distinguished command	Strong Command	Moderate Command	Partial Command	Little Command	
Student work shows distin-	Student work shows strong	Student work shows moderate	Student work shows partial	Student work shows little un-	
guished levels of understand-	levels of understanding of the	levels of understanding of the	understanding of the mathe-	derstanding of the mathemat-	
ing of the mathematics.	mathematics.	mathematics.	matics.	ics.	
Student constructs and com-	Student constructs and com-	Student constructs and com-	Student constructs and com-	Student attempts to constructs	
municates a complete response	municates a complete re-	municates a complete response	municates an incomplete re-	and communicates a response	
based on explana-	sponse based on explana-	based on explana-	sponse based on student's at-	using the:	
tions/reasoning using the:	tions/reasoning using the:	tions/reasoning using the:	tempts of explanations/ reason-	Tools:	
Tools:	Tools:	Tools:	ing using the:	 Manipulatives 	
 Manipulatives 	 Manipulatives 	 Manipulatives 	Tools:	 Five Frame 	
 Five Frame 	 Five Frame 	 Five Frame 	 Manipulatives 	 Ten Frame 	
 Ten Frame 	 Ten Frame 	 Ten Frame 	 Five Frame 	 Number Line 	
 Number Line 	 Number Line 	 Number Line 	 Ten Frame 	 Part-Part-Whole 	
 Part-Part-Whole 	 Part-Part-Whole 	 Part-Part-Whole 	 Number Line 	Model	
Model	Model	Model	 Part-Part-Whole 	Strategies:	
Strategies:	Strategies:	Strategies:	Model	 Drawings 	
 Drawings 	 Drawings 	 Drawings 	Strategies:	 Counting All 	
 Counting All 	 Counting All 	 Counting All 	 Drawings 	 Count On/Back 	
 Count On/Back 	 Count On/Back 	 Count On/Back 	• Counting All	 Skip Counting 	
 Skip Counting 	 Skip Counting 	 Skip Counting 	 Count On/Back 	 Making Ten 	
 Making Ten 	 Making Ten 	 Making Ten 	 Skip Counting 	 Decomposing 	
 Decomposing 	 Decomposing 	 Decomposing 	 Making Ten 	Number	
Number	Number	Number	 Decomposing 	Precise use of math vocab-	
Precise use of math vocab-	Precise use of math vocab-	Precise use of math vocabu-	Number	ulary	
ulary	ulary	lary	Precise use of math vocab-		
Response includes an efficient			ulary	Response includes limited evi -	
and logical progression of Response includes a logical		Response includes a logical but	Desmanae includes are free a	dence of the progression of	
mathematical reasoning and	progression of mathematical	incomplete progression of	Response includes an incom -	mathematical reasoning and	
understanding.	reasoning and understanding.	mathematical reasoning and	plete or illogical progression of	understanding.	
		understanding.	mathematical reasoning and		
E nointe	4 nointe	Contains minor errors.	understanding.	1 noint	
5 points	4 points	3 points	2 points	1 point	

DATA DRIVEN INSTRUCTION

Formative assessments inform instructional decisions. Taking inventories and assessments, observing reading and writing behaviors, studying work samples and listening to student talk are essential components of gathering data. When we take notes, ask questions in a student conference, lean in while a student is working or utilize a more formal assessment we are gathering data. Learning how to take the data and record it in a meaningful way is the beginning of the cycle.

Analysis of the data is an important step in the process. What is this data telling us? We must look for patterns, as well as compare the notes we have taken with work samples and other assessments. We need to decide what are the strengths and needs of individuals, small groups of students and the entire class. Sometimes it helps to work with others at your grade level to analyze the data.

Once we have analyzed our data and created our findings, it is time to make informed instructional decisions. These decisions are guided by the following questions:

- What mathematical practice(s) and strategies will I utilize to teach to these needs?
- What sort of grouping will allow for the best opportunity for the students to learn what it is I see as a need?
- Will I teach these strategies to the whole class, in a small guided group or in an individual conference?
- Which method and grouping will be the most effective and efficient? What specific objective(s) will I be teaching?

Answering these questions will help inform instructional decisions and will influence lesson planning.

Then we create our instructional plan for the unit/month/week/day and specific lessons.

It's important now to reflect on what you have taught.

Did you observe evidence of student learning through your checks for understanding, and through direct application in student work?

What did you hear and see students doing in their reading and writing?



Data Analysis Form	School:	Teacher:		_ Date:
Assessment:			NJSLS:	
GROUPS (STUDENT INITIALS)	SUPPORT PLAN		PROGRESS	
MASTERED (86% - 100%) (PLD 4/5):				
DEVELOPING (67% - 85%) (PLD 3):				
INSECURE (51%-65%) (PLD 2):				
BEGINNING (0%-50%) (PLD 1):				

MATH PORTFOLIO EXPECTATIONS

The Student Assessment Portfolios for Mathematics are used as a means of documenting and evaluating students' academic growth and development over time and in relation to the NJSLS. The September task entry(ies) should reflect the prior year content and *can serve* as an additional baseline measure.

All tasks contained within the **Student Assessment Portfolios** should be aligned to NJSLS and be "practice forward" (closely aligned to the Standards for Mathematical Practice).

Four (4) or more additional tasks will be included in the **Student Assessment Portfolios** for Student Reflection and will be labeled as such.

K-2 GENERAL PORTFOLIO EXPECTATIONS:

- Tasks contained within the Student Assessment Portfolios are "practice forward" and denoted as "Individual", "Partner/Group", and "Individual w/Opportunity for Student Interviews¹.
- Each Student Assessment Portfolio should contain a "Task Log" that documents all tasks, standards, and rubric scores aligned to the performance level descriptors (PLDs).
- Student work should be attached to a completed rubric; with appropriate teacher feedback on student work.
- Students will have multiple opportunities to revisit certain standards. Teachers will capture each additional opportunity "as a new and separate score" in the task log.
- A 2-pocket folder for each Student Assessment Portfolio is recommended.
- All Student Assessment Portfolio entries should be scored and recorded as an Authentic Assessment grade (25%)².
- All Student Assessment Portfolios must be clearly labeled, maintained for all students, inclusive of constructive teacher and student feedback and accessible for review.

GRADES K-2

Student Portfolio Review

Provide students the opportunity to review and evaluate their portfolio at various points throughout the year; celebrating their progress and possibly setting goals for future growth. During this process, students <u>should</u> <u>retain ALL of their current artifacts</u> in their Mathematics Portfolio

2nd Grade Authentic Assessment #1 – Peanuts and Ducks

Peanuts and Ducks

Lee bought a bag of 15 peanuts to feed the ducks. When he got to the lake he saw 6 ducks and 7 more came. He wants to give each duck one peanut.

Part 1:

Does he have enough to give each duck a peanut?

Show how you found the answer using words, numbers, or pictures

Part 2:

How many will be leftover?

Explain your answer using words, numbers, or pictures.

2.NBT.5 Fluently add and subtract within 100 using strategies based on place value, properties of operations,

and/or the relationship between addition and subtraction.

Mathematical Practice 2,6

Individual

SOLUTION: Part A: Yes Correct explanation such as matching peanuts to ducks or 6+8 =13 or 13 + 2 =15 or 15-2= 13				
Level 4: Strong Com- mand			Level 2: Partial Command	Level 1: No Command
Student can an- swer both parts correctly.	swer	one part cor-	Student can only answer one part correctly.	Student can- not re- spond.
Clearly constructs and communicates a com- plete response for at least one part based on explanations/ reasoning using the: • properties of operations • relationship between addi- tion and sub- traction Response includes a logical progression of steps	rectly. Constructs and com- municates a complete response based on explana- tions/reasoning using the: properties of operations relationship between addi- tion and sub- traction Response includes a logical but incomplete progression of steps. Minor calculation er- rors		Constructs and communicates an incomplete re- sponse based on explana- tions/reasoning using the: properties of opera- tions relation- ship be- tween ad- dition and subtrac- tion Response includes	The student shows no work or justification.
	Level 4: Strong Com- mand Student can an- swer both parts correctly. Clearly constructs and communicates a com- plete response for at least one part based on explanations/ reasoning using the: • properties of operations • relationship between addi- tion and sub- traction Response includes a logical progression of	Level 4: Strong CommandLevel CommandStudent can answer both parts correctly.Student can answer both parts correctly.Student can answer both parts correctly.Clearly constructs and communicates a complete response for at least one part based on explanations/ reasoning using the:Const municates a complete response for at least one part based on explanations/ reasoning using the:• properties of operations of relationship between addition and subtraction•• Response includes a logical progression of stepsResponse includes a logical progression of steps	Level 4: Strong CommandLevel 3: Moderate CommandStudent can an- swer both parts correctly.Student can only an- swer one part cor- rectly.Clearly constructs and communicates a com- plete response for at least one part based on explanations/ reasoning using the:Constructs and com- municates a complete response based on explana- tions/reasoning using the:• properties of operations • relationship between addi- tion and sub- traction• properties of operations • relationship between addi- tion and sub- tractionResponse includes a logical progression of steps• non- response includes a logical progression of steps. Minor calculation er-	Or 13+2 =15Level 4: Strong CommandLevel 3: Moderate CommandLevel 2: Partial CommandStudent can answer both parts correctly.Student can only answer one part correctly.Student can only answer one part correctly.Clearly constructs and communicates a complete response for at least one part based on explanations/ reasoning using the:Constructs and communicates a complete response based on explana- tions/reasoning using the:Constructs and communicates an complete response based on explana- tions/reasoning using the:Constructs and communicates an incomplete re- sponse based on explana- tions/reasoning using the:Constructs and communicates an incomplete re- sponse based on explana- tions/reasoning using the:Constructs and communicates an incomplete re- sponse based on explana- tions/reasoning using the:•properties of operations••properties of opera- tions•properties of operations••properties of opera- tions•relationship between addi- tion and sub- traction••••Response includes a logical progression of steps. Minor calculation er-••••Response includes•Respo

Core Instructional and Supplemental Materials (K-5)

EUREKA MATH V. 2019 (GREAT MINDS)

GRADE	TEACHER RESOURCES	STUDENT RESOURCES
K (v. 2019.)	 Teacher Edition: Module 1-6 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-6 Succeed Workbook Set: Module 1-6 Practice Workbook, Fluency: Module 1-6
1	 Teacher Edition: Module 1-6 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-6 Succeed Workbook Set: Module 1-6 Practice Workbook, Fluency: Module 1-6
2	 Teacher Edition: Module 1-8 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-8 Succeed Workbook Set: Module 1-8 Practice Workbook, Fluency: Module 1-8
3 4	 Teacher Edition: Module 1-7 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-7 Succeed Workbook Set: Module 1-7 Practice Workbook, Fluency: Module 1-7
5	 Teacher Edition: Module 1-7 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-7 Succeed Workbook Set: Module 1-7 Practice Workbook, Fluency: Module 1-7
	 Teacher Edition: Module 1-6 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-6 Succeed Workbook Set: Module 1-6 Practice Workbook, Fluency: Module 1-6

MATH IN FOCUS v. 2015

(HOUGHTON MIFFLIN HARCOURT)

GRADE	TEACHER RESOURCES	STUDENT RESOURCES
К	 Teacher Edition (A & B) Implementation Guide Assessment Package Enrichment Bundle Extra Practice Set Teacher and Student Activity Cards Home -to- School Connection Book Online Teacher Technology Kit Big Book Set Online Interactive Whiteboard Lessons 	 Student Edition A – Pt. 1 Student Edition A – Pt. 2 Student Edition B – Pt. 1 Student Edition B – Pt. 2 Online Student Technology Kit
1	 Teacher Edition (A & B) Implementation Guide Assessment Package Enrichment Bundle Extra Practice Guide Reteaching Guide Home -to- School Connection Book Online Teacher Technology Kit Fact Fluency Online Interactive Whiteboard Lessons 	 Student Texts (A & B) Student Workbooks Online Student Technology Kit Student Interactivities
2-5	 Teacher Edition (A & B) Implementation Guide Assessment Package Enrichment Bundle Extra Practice Guide Transition Guides Reteaching Guide Home -to- School Connection Book Online Teacher Technology Kit Fact Fluency Online Interactive Whiteboard Lessons 	 Student Texts (A & B) Student Workbooks Online Student Technology Kit Student Interactivities

Supplemental Resources

Great Minds https://greatminds.org/

Embarc https://embarc.online/

Engage NY http://www.engageny.org/video-library?f[0]=im_field_subject%3A19

Common Core Tools <u>http://commoncoretools.me/</u> <u>http://www.ccsstoolbox.com/</u> <u>http://www.achievethecore.org/steal-these-tools</u>

Achieve the Core http://achievethecore.org/dashboard/300/search/6/1/0/1/2/3/4/5/6/7/8/9/10/11/12

Manipulatives http://nlvm.usu.edu/en/nav/vlibrary.html

http://www.explorelearning.com/index.cfm?method=cResource.dspBrowseCorrelations&v=s&id=USA-000

http://www.thinkingblocks.com/

Illustrative Math Project : http://illustrativemathematics.org/standards/k8

Inside Mathematics: <u>http://www.insidemathematics.org/index.php/tools-for-teachers</u>

Sample Balance Math Tasks: <u>http://www.nottingham.ac.uk/~ttzedweb/MARS/tasks/</u>

Georgia Department of Education: https://www.georgiastandards.org/Common-Core/Pages/Math-K-5.aspx

Gates Foundations Tasks:<u>http://www.gatesfoundation.org/college-ready-education/Documents/supporting-instruction-cards-math.pdf</u>